

**Title: Forward Error Correction (FEC) on a Link
Between ICs**

5 Field of the Invention

The present invention relates generally to high-speed transport networks and, more particularly, to the transmission of signals on backplanes and between ICs on a same circuit pack using error correction techniques for reducing bit error rates at high transmission speeds.

Background

At relatively low speeds of data transportation, roughly 100 Mb/sec, error rates between two different ICs on a circuit pack or over a backplane are generally unmeasurable. In other words, they are close to zero. As speeds of data transportation over backplanes and between ICs increase to 2.5 Gb/s and above, the likelihood of having transmission errors increases as well. These errors may be due to effects such as inter-symbol interference, attenuation, couplings between links on the ICs, noise coupling from digital to analog section of an IC, simultaneous switching noise in ICs, signal distortion in connectors or backplane, and process distortion, among others. Consequently, it becomes difficult to get sufficiently low errors rates.

Consequently, there is a need in the industry for reducing bit error rates at high transmission speeds over backplanes and between ICs.

Summary of the Invention

5 In accordance with a broad aspect, the invention provides the use of forward error correction data in a signal carried over a link between two ICs (Integrated Circuits). In a non-limiting example, the link between two ICs is between two ICs on a same circuit pack.
10 Alternatively, the link between two ICs includes a backplane.

In a specific example, the link between two ICs is a medium suitable for the propagation of electrical signals.

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In accordance with another broad aspect, the invention provides a method for generating a signal for transmission over a link between two ICs. An input signal is received, the input signal comprising payload data to be transmitted
20 over the link between two ICs. The data in the input signal is processed to derive forward error correction data at least on part on the basis of the payload data in the input signal. An output signal comprising the payload data received in the input signal and the forward error
25 correction data is then generated and released for transmission over the link between two ICs.

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In a specific example, the link between two ICs can include a backplane or a link between two ICs on a same circuit pack.

In accordance with another broad aspect, the invention provides an apparatus for implementing the above-described method.

5 In accordance with another broad aspect, the invention provides a signal carried over a link between two ICs. The signal includes a sequence of frames, each frame including a plurality of sequential blocks, each block being characterized by a compound data structure suitable for carrying payload data and overhead information. The compound data structure is derived by bit-multiplexing a set of N primary data structures. Each primary data structure comprises a first portion and a second portion, the first portion including payload data, the second portion including forward error correction data derived from the data elements in the first portion.

10 In a non-limiting specific example of implementation, the signal has a rate of about 2.5 Gb/s and comprises a sequence of frames, each frame includes 1 framing pattern and 66 sequential blocks. Each block being characterized by a compound data structure, where the compound data structure is derived by bit-multiplexing a set of 4 primary data structures. In other words $N=4$. The skilled person in the art will readily appreciate that N can take on a plurality of non-negative integer number values greater than 0. In a non-limiting example, N is selected from the set consisting of {1, 2, 3, . . . , 14, 15, 16}. Each primary data structure includes about 1176 bits, wherein at least part of the first 1164 bits of each primary data structure includes payload data, and 12 bits include forward error correction.

It will be readily appreciate that any suitable coding may be applied to the payload data in a given block to derive the forward error correction data for that given block. In a very specific non-limiting example, the forward error correction data in a given primary data structure are derived by applying BCH-1 coding on at least part of the payload data of the given primary data structure. The skilled person in the art will readily appreciate that methods, other than BCH-1 coding, may be used in connection with FEC without detracting from the spirit of the invention.

In accordance with another broad aspect, the invention provides a method and an apparatus for generating the above-described signal for transmission over a link between two ICs. The link between two ICs may include a backplane or a link between two ICS on a same circuit pack.

In accordance with another broad aspect, the invention provides an IC suitable for processing a signal of the type described above. Processing a signal comprises plurality of signal processing functions including but not limited to signal generation and signal information extraction.

Other aspects and features of the present invention will become apparent to those ordinarily skilled in the art upon review of the following description of specific embodiments of the invention in conjunction with the accompanying figures.

Brief Description of the Drawings

Fig. 1 is a specific example of an apparatus for generating a signal constructed in accordance with a specific example of implementation of the invention;

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Fig. 2 is a detailed block diagram of the processing unit in the apparatus of figure 1;

Fig. 3 depicts a primary data structure in accordance with a specific example of implementation of the invention;

Fig. 4 shows a compound data structure in accordance with a specific example of implementation of the invention;

Fig. 5 depicts a signal characterized by a digital signal frame format providing forward error correction in accordance with a specific example of implementation of the invention;

Fig. 6 is a specific example of an apparatus for extracting information from a signal constructed in accordance with a specific example of implementation of the invention;

Fig. 7 is a detailed block diagram of the processing unit in the apparatus of figure 6;

Fig. 8 is a block diagram of a specific example of implementation of the apparatuses of figures 1 and 6.

In the drawings, embodiments of the invention are illustrated by way of example. It is to be expressly understood that the description and drawings are only for

purposes of illustration and as an aid to understanding, and are not intended to be a definition of the limits of the invention.

5 Detailed Description

10 The specific example of implementation described pertains to apparatuses for exchanging signals over a link between two ICs, the link being capable of propagating electrical signals.

15 Figure 1 shows an apparatus 100 suitable for transmitting signals over a link between two ICs 112. In a non-limiting example, the link between two ICs 112 includes a backplane portion. Alternatively, link 112 is a link between two ICs on a same circuit pack. As depicted, the apparatus 100 comprises an input 114, an output 116, a processing unit 102, and a transmit interface 110.

20 The input 114 is for receiving payload data from one or more functional processing units. The payload data may be in any suitable format. The functional processing units may reside on the same physical structure as apparatus 100
25 or on a different physical structure. In a non-limiting example, the physical structure is an electronic circuit such as an ASIC (Application Specific Integrated Circuit). The specific functional processing units from which the data originates does not form part of the invention and as
30 such will not be described.

The processing unit 102 processes the payload data in the input signal received at input 114 to derive associated

forward error correction data. The processing unit then generates an output signal comprising the payload data and the generated forward error correction data.

5 The interface 110 receives the output signal generated by the processing unit 102 and performs any necessary processing for transmitting the output signal over the link between two ICs 112. This may include for example multiplexing from a parallel bus to a serial bit stream.

10 The functionality of processing unit 102 will now be described in accordance with a specific example of implementation with reference to figure 2 of the drawings.

15 In accordance with a specific implementation, as depicted in figure 2, the processing unit 102 includes a set of N forward error correction (FEC) calculator units 200 202 204 206, a bit-multiplexor 208 and a framing pattern generator 210.

20 In a typical interaction, a signal including payload is received by processing unit 102 from input 114. The skilled person in the art will readily appreciate that different types of payload data may be received from port
25 114 without detracting from the spirit of the invention.

30 The payload data may be comprises of N channels or of a single channel. This specific example considers the case where the input signal is comprises of N channels. Each of the N channels is directed to a respective FEC calculator unit 200 202 204 206. At each FEC calculator unit, forward error correction data is computed on the basis of payload

data. Many different FEC schemes may be used here. In a
~~very specific example of implementation, the FEC scheme is~~
a 1st order Binary BCH code. Advantageously, this FEC
scheme allows the FEC decoder at the receiver to correct up
5 to 1 error per primary data structure. Each FEC calculator
unit then generates a primary data structure. Each primary
data structure comprises a first portion and a second
portion, the first portion including payload data, the
second portion including forward error correction data
10 derived from the data elements in the first portion. A
representation of a specific implementation of the primary
data structure is depicted in figure 3. In the specific
implementation depicted in figure 3, each primary data
structure includes 1176 bits. In the primary data structure
15 300, the payload data 302 occupies bits 1-1164, the forward
error correction data 304 occupies 12 bits namely bits
1165-1176.

In this fashion a set of N primary data structures is
20 generated by the set of N FEC calculator units. In a
variant, the N primary data structures may be generated
serially by taking N sequential portions of the payload
data received at input 114 on a same channel. In this
variant, a single FEC calculator unit may be used. The N
25 primary data structures are then transmitted to the bit-
multiplexor unit 208.

The bit-multiplexor unit 208 bit-multiplexes the set
of N primary data structures to generate a compound data
30 structure. A representation of a specific implementation of
the primary data structure is depicted in figure 4. The
compound data structure 408 shown in figure 4 is derived by

bit-multiplexing a set of $N=4$ primary data structures 400
402 404 and 406 similar in format to primary data structure
300. The skilled person in the art will readily appreciate
that N can take on a plurality of non-negative integer
5 number values greater than 0. In a non-limiting example, N
is selected from the set consisting of $\{1, 2, 3, \dots, 14,$
15, 16 $\}$. As shown, the compound data structure comprises
payload data and forward error correction data. More
specifically, the compound data structure comprises 582
10 bytes (582 8-bit words) of payload data and 6 bytes of
forward error correction data 414. The manner in which the
bit-multiplexor multiplexes the primary data structure may
vary widely from one implementation to the other.

15 The table below shows a non-limiting specific
implementation of the bit-multiplexing mapping.

Compound data structure Bit numbering	Bits mapped from the 4 channels
Bit #1	bit 1,3 ... 1175 of primary data structure #1
Bit #2	bit 1,3,... 1175 of primary data structure #2
Bit #3	bit 1,3,... 1175 of primary data structure #3
Bit #4	bit 1,3,... 1175 of primary data structure #4
Bit #5	

Compound data structure Bit numbering	Bits mapped from the 4 channels
	bit 2,4,... 1176 of primary data structure #1
Bit #6	bit 2,4,... 1176 of primary data structure #2
Bit #7	bit 2,4,... 1176 of primary data structure #3
Bit #8	bit 2,4,... 1176 of primary data structure #4

On the basis of the above table, word #1 identified as element 410 in figure 4, comprises of bits #1 and #2 of the primary data structures 400 402 404 and 406, while word #2 identified as element 412 in figure 4, comprises of bits #3 and #4 of the same primary data structures. Advantageously, bit multiplexing allows a burst of bit errors to be spread amongst the interleaved primary data structures, therefore increasing the likelihood that a given primary data structure will have no more than 1 bit error.

The compound data structure is then transmitted to the frame generation unit 210. The frame generation unit 210 generates a sequence of frames at least in part on the basis of the compound data structures received from the bit-multiplexor unit 208. Each frame includes a framing pattern and a plurality of sequential blocks, each block being characterized by a compound data structure. For each

K blocks, a framing pattern identifying frame boundaries is added. The framing pattern may be in any suitable format.

Figure 5 shows a specific example of a digital signal frame format providing forward error correction. The frame 500 and includes 66 compound data structure blocks 510 and a framing pattern 512. Each block 510 in the frame 500 is characterized by a compound data structure of the type depicted in figure 4. At the beginning of each frame, a framing pattern is appended and is designated with reference numeral 512. It will be readily apparent that the framing pattern may alternatively be appended anywhere in the frame without detracting from the spirit of the invention. The framing pattern 512 occupies 72 bytes and is a fixed pattern used to identify frame boundaries. The frames generated by the frame generation unit are then forwarded to the transmit interface 110.

The transmit interface 110 releases a signal including a sequence of frames at the output 116 for transmission over the link between two ICs 112, each frame including a plurality of sequential blocks, each block being characterized by a compound data structure suitable for carrying payload data and overhead information. The compound data structure is derived by bit-multiplexing a set of N primary data structures, each primary data structure having a first portion and a second portion. The first portion of the primary data including payload data and the second portion including forward error correction data derived from the data elements in the first portion.

In a specific example of implementation, the signal carrying the frame 500 over link between two ICs 112 has a rate of about 2.5Gb/s. The expression about 2.5Gb/s may be used to include line rates in the ranges between about 2 Gb/s and about 3 Gb/s, between about 2.4 Gb/s and about 2.8 Gb/s and between about 2.5 Gb/s and about 2.7 Gb/s. In this example, each frame in the transmitted signal has a duration of about 125 μ s.

Figure 6 shows an apparatus 600 suitable for receiving signals from the link between two ICs 112. As depicted, the apparatus 600 comprises an input 616, an output 614, a processing unit 602, and a receive interface 610.

The receive interface 610 receives the signal originating from the link between two ICs 112 and performs any necessary processing for transmitting the output signal to the processing unit 602. The signal received has a rate of about 2.5 Gb/s and comprises a sequence of frames. The receive interface 610 performs any necessary conversions between the signal on the link between two ICs 112 and the signal to be received by the processing unit 602. In a specific implementation, the receive interface 610 applies to the signal the inverse processing operation that was applied by the transmit interface 110 of figure 1. In a non-limiting example, the receive interface 110 may provide amplification, equalization, decision circuitry to translate analog voltage level to binary 1 or 0 and clock recovery circuit, amongst others.

The processing unit 602 processes the signal received from the receive interface 110 to extract payload data to

be transmitted to one or more functional processing units. The output 614 is for transmitting payload data extracted by the processing unit 602 to one or more functional processing units.

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The functionality of processing unit 602 will now be described in accordance with a specific example of implementation with reference to figure 7 of the drawings.

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In accordance with a specific implementation, as depicted in figure 7, the processing unit 602 includes a set of N forward error correction (FEC) processing units 700 702 704 706, a bit de-multiplexor unit 708 and a frame extraction unit 710.

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The frame extraction unit 710 is suitable for receiving a signal including frames of the type depicted in figure 5. The frame extraction unit 710 locks in on the framing pattern in order to determine frame boundaries and block boundaries, each block being characterized by a compound data structure. The framing pattern is then removed from the frame and the blocks are forwarded to the

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bit de-multiplexor 708.

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The bit de-multiplexor unit 708 applies to each compound data structure the inverse of the multiplexing operation applied by the bit multiplexor unit 208 shown in figure 2 in order to derive N primary data structures.

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In the specific example depicted in the drawings, the compound data structure of the type shown in figure 4 is bit de-multiplexed into a set of N=4 primary data

structures similar in format to primary data structure 300. The skilled person in the art will readily appreciate that N can take on a plurality of non-negative integer number values greater than 0. In a non-limiting example, N is
5 selected from the set consisting of {1, 2, 3, . . . , 14, 15, 16}. Each primary data structure comprises a first portion and a second portion, the first portion including payload data, the second portion including forward error correction data derived from the data elements in the first portion.
10 Each of the N primary data structures is then forwarded to a respective forward error correction (FEC) processing unit. This specific example considers the case where the payload data is associated to N channels. In a variant, where the N primary data structures include data
15 originating from a same channel, a single FEC processing unit may be used and the N primary data structures are forwarded to the same FEC processing unit.

The FEC processing units 700 702 704 706 receive
20 respective primary data structures. Each FEC processing units decodes the FEC portion of the primary data structure and effects any required correction to the payload data portion. The specific FEC decoding function applied by the FEC processing units is dependent upon the FEC coding used
25 by FEC calculator units 200 202 204 and 206. Advantageously, the use of FEC over a link between two ICs allows a reduction in the bit error rate (BER) when transmitting a signal over a backplane or between two ICS on a same circuit pack. The FEC processing units 700 702
30 704 706 then release a signal including payload data to output 614. The skilled person in the art will readily appreciate that different types of payload data may be

released at output 614 without detracting from the spirit of the invention.

5 The above-described apparatuses 100 600 for generating and receiving a signal of the type described in connection with figure 5 can be implemented on devices including a microprocessor 802 and a memory 803 as shown in figure 8. The microprocessor 802 is adapted to execute a program element 806 in order to implement the functional blocks described in the specification and depicted in the drawings. Alternatively, the above-described apparatuses 100 600 can be implemented on a dedicated hardware platform where electrical/electronic components implement the functional blocks described in the specification and depicted in the drawings.

10 The apparatuses 100 may form part of an integrated circuit imbedded in a dedicated chip or may form part of an IC.

20 It is to be appreciated that although the reception and transmission capabilities have been described with reference to figures 1 and 6 as implemented by separate apparatuses, it will be readily apparent that a same apparatus including both transmission and reception capability falls within the scope of the invention.

25 Although the present invention has been described in considerable detail with reference to certain preferred embodiments thereof, variations and refinements are possible without departing from the spirit of the

invention. Therefore, the scope of the invention should be limited only by the appended claims and their equivalents.

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